Acta Cryst. (1967). 23, 754

The Crystal Structure of NaTi₂Al₅O₁₂

BY W.G. MUMME AND A.D. WADSLEY

Division of Mineral Chemistry, C.S.I.R.O., Melbourne, Australia

(Received 31 January 1967)

NaTi₂Al₅O₁₂, a new compound prepared by solid-state reaction, crystallizes as colourless orthorhombic needles with the unit-cell dimensions a=9.080, b=15.519, c=2.919 Å, space group *Pbam*. The composition was deduced from the structure analysis, which proceeded by Patterson and Fourier methods to refinement of three-dimensional data by the method of least squares. The structure contains double strings of octahedra, one with aluminum and the other titanium joined by corners into sheets. These are further cross-linked by two additional aluminum polyhedra, an octahedron and a tetrahedron, while sodium occupies a flattened octahedral position between the double strings. The temperature factor for Na is anomalous, and the possible reasons for this are evaluated.

Introduction

Examination of alkali titanates in this laboratory showed that a characteristic and unifying feature for three compounds, $Na_2Ti_3O_7$, $Na_2Ti_6O_{13}$ and Ti_3O_5 was a condensed group of Ti–O octahedra sharing edges, three wide, and extending as an infinite zigzag unit throughout the structure of each one (Andersson & Wadsley, 1962*a*).

Additional arrangements of these groups can be devised which might represent hitherto unknown chemical compounds, the compositions being determined by counting atoms within the unit cells of their predetermined structures. In the course of unsuccessful attempts to prepare a fourth related phase Na₂Ti₄Al₂O₁₂, isostructural with a 'bronze' Na₂Ti₆O₁₂, we isolated a number of colourless orthorhombic needles which were formed together with a second aluminotitanate belonging to another bronze structure type, Na_xTiO₂ (Andersson & Wadsley, 1962b; Bayer & Hoffmann, 1965). These proved to be an unsuspected new phase with the ideal composition NaTi₂Al₅O₁₂.

Experimental

The compound is readily made by heating an intimate mixture of Na₂CO₃, Al₂O₃ and TiO₂ (anatase) in the molar ratio 1:5:4, first at 800 °C in air and then in a sealed capsule at 1300 °C for 48 hours.

It is characterized by its powder pattern (Table 1). The crystallographic data, summarized in Table 2, were determined from a Guinier film internally calibrated with potassium chloride, and the space group alternatives from single-crystal photographs. Intensity data hkl for the levels l=0, 1, 2, were obtained by the integrated Weissenberg technique using filtered copper radiation, the crystal measuring $0.1 \times 0.02 \times 0.015$ mm. Corrections for absorption were found to be unnecessary. Intensities were measured visually with a standard scale, and the reduction to structure amplitudes, and all subsequent computing, was carried out on the

Division's Elliott 803 computer using the programming system devised by Daly, Stephens & Wheatley (1963) and kindly made available to us by Dr P.J. Wheatley. Interlayer scaling for the three levels of data was adjusted after each least-squares refinement cycle, and the scaled observed data and the structure amplitudes calculated from the final model are listed in Table 3. Scattering curves for non-ionized atoms, corrected for the real and imaginary components of the anomalous scattering for Cu $K\alpha$, were taken from International Tables for X-ray Crystallography (1962, p. 201 et seq.).

Table 1. Powder pattern of NaTi₂Al₅O₁₂, Cu Ka₁

I (obs)	$\sin^2 \theta$ (obs)	$\sin^2 \theta$ (calc)	hkl
mw	0.00964	0.00966	110
w	0.00984	0.00985	020
mw	0.01703	0.01705	120
m	0.02938	0.02937	130
vw	0.03937	0.03942	040
5	0.06823	0.06820	240
m	0.08699	0.08694	330
m	0.09842	0.09843	201
mw	0.09898	0.09901	131
vw	0.10832	0.10828	221
w	0.10906	0.10906	041
m	0.12068	0.12060	231
m	0.14952	0.14950	270
mw	0.17375	0.17383	341
ms	0.20281	0.20383	460

Table 2. Crystallographic data for NaTi₂Al₅O₁₂

Symmetry:	orthorhombic
Unit-cell dimensions	$a = 9.080 \pm 0.005 \text{ Å}$ $b = 15.519 \pm 0.005$ $c = 2.919 \pm 0.002$
Systematically absent reflexions	$\begin{array}{l} 0kl, \ k \neq 2n \\ h0l, \ h \neq 2n \end{array}$
Possible space groups	Pba2 (no. 32) Pbam (no. 55)
D_x Z	3.60 g.cm^{-3}
$-\mu_c$	114 cm ⁻¹

Structure determination

The c-axis length of 2.92 Å corresponds in all probability to an oxygen-to-oxygen distance which will be an octahedral or tetrahedral edge. As all the atoms should be resolved in projection on to (001), where both space group alternatives Pbam and Pba2 are centred, the structure determination by Fourier meth-



Fig.1. Projection of the Patterson function, P(u, v), positive regions only. The zero contour is dotted.

ods was confined to the hk0 level, and all the data were used subsequently for the refinement by leastsquares.

Apart from the question of chemical composition, which at this stage was uncertain, the interpretation of the Patterson function, P(u,v), shown in Fig.1, proved unexpectedly troublesome. An examination of it suggested a trial structure where the approximate locations of three metal atoms in general fourfold positions, A at (0.22, 0.14), B at (0, 0.29) and C at (0.28, 0.36), all centred about the point $(\frac{1}{4}, \frac{1}{4})$, were determined from the strongest vector interactions when an additional metal was placed in the special twofold site at (0,0). Because the exact composition was unknown, and because it did not seem feasible at this stage to attempt to distinguish between any of these four positions, an averaged scattering curve for aluminum and titanium was used for calculating structure factors with this model. This had the effect of retaining the additional symmetry elements, to make the plane group cmm rather than the correct one pgg. While this resulted in poor overall agreement between the observed and calculated structure factors (because in cmm the terms F_{hk0} are zero when h+k=2n+1), a two-dimensional

Table 3. Observed and calculated structure factors

b	k l	L Fat	100)	Fc (x100)	b	k	L	F ₀ (x100)	F _C (x100)	I	b	k	ι	F ₀ (x 100)	F _c (x100
000001111112222222222222222222222222222	2 4 6 9 4 8 1 2 7 5 7 0 2 7 4 7 9 0 7 6 8 1 2 7 4 5 6 7 8 5 6 7 8 5 6 7 8 5 6 7 8 5 6 7 8 7 8 7 9 7 9 7 1 2 7 7 1 2 5 0 7 5 9 0 1 7 1 2 6 7 8 1 2 0 1 3 5 6 7 8 1 2 7 5 6 7 8 1 2 7 1 2 7 7 1 2 7 7 1 2 5 0 7 5 9 0 1 7 1 2 6 7 8 1 2 0 1 3 5 6 7 8 1 2 7 5 6 7 8 1 2 7 1 2 7 7 7 1 2 7	٥٥٥٥٥٥٥٥٥٥٥٥٥٥٥٥٥٥٥٥٥٥٥٥٥٥٥٥٥٥٥٥٥٥٥٥٥	7527747737373731737216557521695752193947519191910753551591182551551555557574745675155575757552125755555555555555555555	K4 n 44 990 m 21 5 2 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	001110000000111111111222222222222222222	ບອນບາດ ລະເອ ດີສາຄີ ທາງປະກິນການການເປັນການການເປັນ ຄຳມາຍປະເທດ ແລະ ຄຳມາຍາດ ແລະ ແລະ ແລະ ແລະ ແລະ ແລະ ແລະ ແລະ ແລະ ແ	000017777777777777777777777777777777777	90000339900379971224866911339047171739171749475475475475974780731148165531204716826596897479454567548967479478 73033899003799722252675757555485201164146655700726475447174759714476597492375457522124220847479547548965479124 73127772222575757555555555548252011641465557007264754754759747829747823555555120212422084745954555552022555	772757964713777075777075777075777075772777777777777		000000011111112222222222223333333333333	**************************************	๛๛๛๛๛๛๛๛๛๛๛๛๛๛๛๛๛๛๛๛๛๛๛๛๛๛๛๛๛๛๛๛๛๛๛๛	2724788273748797891167916901429757494372676670017673732875866398675077028282782826759122166247221 2922788273748794891167169267279583939393939393939393939393939393939393	~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~

electron density projection on to (001), containing only the terms h+k=2n, verified all the metal positions and showed that an additional metal atom was at $(0, \frac{1}{2})$. The interpretation of the forthcoming oxygen structure was complicated by the doubling of each oxygen peak by reproduction across the pseudo-centre at $(\frac{1}{4}, \frac{1}{4})$. Guided, however, by their spatial arrangement around the metals, we were able to fix the oxygen positions by choosing an appropriate set of peaks for each half of the asymmetric unit, and thereby restoring the correct symmetry.

With the oxygen structure interpreted in this manner, it became apparent that the metal at (0.28, 0.36)was tetrahedrally coordinated. Taken into consideration with the smaller size of its peak when another F_{hk0} projection was computed, this seemed most likely to be an aluminum atom, while its counterpart across the pseudo-centre was octahedral titanium. From the size of their electron density peaks, the atoms at (0,0)and (0,0.29) were also aluminum, both octahedrally coordinated, so that the remaining atom appearing at $(0,\frac{1}{2})$ was necessarily sodium, thus satisfying a formula $NaTi_2Al_5O_{12}$ for the compound.

Electron density projections on to (001) were used to refine this structure (Fig.2) and continued with a number of least-squares cycles with the two-dimensional data, using isotropic temperature factors for each atom, until R dropped to 8.7%. The weighting scheme of Cruickshank, Pilling, Bujosa, Lovell & Truter (1961) was adopted, and the matrix inversion involved the block-diagonal approximation.

At this stage the hk1 and hk2 data were included, it being assumed that the atoms were situated on the mirror planes at z=0 and $\frac{1}{2}$ of the space group *Pbam*, one aluminum at the origin in 2(a), sodium at 2(d)and each of the remaining atoms in either of 4(h) or 4(g). The isotropic temperature factor for Na proved to be troublesome, rising to an extremely high value of 8 Å⁻², with an R value of 12.2%. A three-dimensional electron density section (0, y, z) showed it to be in 2(d), but the contours were elongated along the c direction.

These two effects could have arisen for a number of reasons. In the first instance the Na might be incorrectly placed in its octahedral environment, and indeed it is possible to give it an alternative tetrahedral position by assigning it to the 2(b) position of *Pba2*, *i.e.* at $0\frac{1}{2}z$, $\frac{1}{2}0z$ with $z = \frac{1}{4}$. Sodium has this configuration in the two isostructural compounds β -NaFeO₂ (Bertaut & Blum, 1954) and NaAlO₂ (Théry, Lejus, Briançon & Collongues, 1961). This reduction of symmetry group freed all the atoms from the mirror planes perpendicular to the c axis, and a number of least-squares refinement cycles, including anisotropic thermal factors. moved them all appreciably. Not only did the internuclear distances become unrealistic but the temperature factor for Na worsened, and consequently this model was abandoned.

A second possibility is to retain the space group Pbam and assume that the two Na atoms in the unit cell statistically occupy the eightfold positions x, y, z, with $x=0, y=\frac{1}{2}, z=\frac{1}{4}$. This places one half Na in each of $0, \frac{1}{2}, \frac{1}{4}$; $0, \frac{1}{2}, \frac{3}{4}$; $\frac{1}{2}, 0, \frac{3}{4}$. Local ordering can now be imagined, with Na occupying one position, $0, \frac{1}{2}, \frac{1}{4}$ in one series of the structural tunnels, whereas it adopts as an alternative either $0, \frac{1}{2}, \frac{3}{4}$ or $\frac{1}{2}, 0, \frac{3}{4}$ in the next unit cell or in the symmetry-related equivalent position. Despite the plausibility of this model, which is supported by evidence from a number of related systems



Fig.2. Electron density projection on to (001), contoured at intervals of three electrons, with zero dotted.

Table	4.	Fractional	atomic	coordinates	and t	hermal	parameters
-------	----	------------	--------	-------------	-------	--------	------------

E.s.d.'s are given in brackets.

	Space group <i>Pbam</i> (no. 52)				Mean-square-amplitude tensors						
	Point position	x		z	<i>U</i> ₁₁	U ₂₂	U ₃₃	2 <i>U</i> ₁₂	2 <i>U</i> ₂₃	2 <i>U</i> ₁₃	
Na	2(d)	0	+	ł	0.052 (20)	0.038 (23)	0.129 (25)	-0.002(25)	0	0	
Al(1)	2(a)	0	Õ	Õ	0.005 (5)	0.012(5)	0.003(9)	-0.005(9)	ŏ	ŏ	
Al(2)	4(g)	0.0098 (9)	0.2999(5)	0	0.011 (5)	0.016 (6)	0.017(9)	-0.006(10)	ŏ	ŏ	
Al(3)	4(h)	0.3069 (9)	0.3553 (7)	ł	0.005 (8)	0.004(7)	0.024(13)	0.004(12)	õ	ŏ	
Ti	4(h)	0.2294 (6)	0.1449 (4)	Ĵ.	0.016(3)	0.019(4)	0.020(6)	-0.005(7)	õ	ŏ	
O(1)	4(h)	0.1050 (19)	0·0513 (13)	ĩ	0.005(12)	0.009(14)	0.025(20)	-0.019(21)	õ	ŏ	
O(2)	4(g)	0.3638 (20)	0.1108(14)	Ô	0.012(13)	0.016(14)	0.025(19)	-0.010(24)	ŏ	ŏ	
O (3)	4(g)	0.1319(22)	0.2059 (14)	Õ	0.019(14)	0.027(17)	0.008(23)	-0.036(24)	ŏ	ŏ	
O(4)	4(h)	0.3902 (24)	0.2481(14)	1	0.016(14)	0.014(16)	0.035(24)	-0.011(20)	ŏ	ň	
O(5)	4(h)	0.1100(22)	0.3534 (16)	Î	0.027(15)	0.026(18)	0.032(24)	0.005(30)	ŏ	ŏ	
0(6)	4(g)	0.3662(21)	0.4072(14)	ó	0.016(14)	0.027(16)	0.025(21)	0.002(26)	ŏ	õ	

(Wadsley, 1964), the temperature factor for Na did not improve.

A third possibility is the fractional occupancy by Na of the positions available to it. If there is less than the stoichiometric amount of Na, the composition would be balanced by replacing a fraction of the octahedral Al by Ti according to the formula $Na_{1-x}Ti_2(Al_{5-x}Ti_x)$ -O₁₂. This would be reflected in the temperature factors of these atoms, which appear, however, to be normal.

Finally the temperature effects might be real. Several least-squares cycles, run with anisotropic temperature factors, soon reached a steady state, U_{33} for Na being the only anomaly. The final *R* value for the observed data was 9.7%. The positional and thermal parameters are listed in Table 4 and the bond lengths in Table 5. Reliance on interatomic distances in specific directions to an accuracy better than the component $(U_{tj})^{\pm}$ cannot be claimed, and the standard deviations of the Na–O bonds in Table 5 are very much underestimated.

The decision between partial occupancy, distribution statistics or large amplitudes of thermal motion is extremely difficult to make unambiguously by crystallographic methods alone. This dilemma has also arisen in a number of additional mixed metal oxides containing alkali, trivalent and quadrivalent metals that we are currently studying, and the structure of a new high-temperature non-stoichiometric phase $Na_xFe_xTi_{2-x}$ (0.90 > x > 0.75) is relevant to the present case. Here one component of the anisotropic thermal corrections for Na is also very large, which once again corresponds to the direction of elongation of the open tunnels in which these ions are sited (Mumme & Reid, 1967). We believe that this oscillation of Na is permitted by its freedom to move relatively unhindered within the tunnels created by the rigid framework, an effect which may prove to be a general feature for this class of compound.

Description

The structure is illustrated by Figs. 3 and 4. There are four crystallographically non-identical octahedral sites, two aluminum, one titanium and one sodium, as well as one tetrahedral aluminum. The six Ti–O bonds vary between 1.84 and 2.17 Å (Table 5) which is normal. The octahedral Al(2)–O distances range from 1.83 to 1.97 Å. These two atoms with their ligands constitute the backbone of the structure, forming a double string by edge-sharing and elongated along the z direction,

Table 5. Interatomic distances and e.s.d.'s (Å)

Al(1) - O(1)	1.915 ± 0.015 (4)	Al(2)-O(3)	1.830 ± 0.018 (1)	Al(3)-O(6)	1·750±0·019 (2)	TiO(1)	1.843 ± 0.016 (1)
Al(1)–O(6')	1.885 ± 0.018 (2)	Al(2) - O(2')	1.916 ± 0.018 (1)	Al(3) - O(5)	1.790 ± 0.021 (1)	TiO(4)	2.167 ± 0.019 (1)
O(1) - O(1')	2.48 ± 0.02 (2)	Al(2)-O(5)	1.910 ± 0.020 (2)	Al(3)–O(4)	1·827±0·020 (1)	TiO(2)	1.973 ± 0.017 (2)
O(1) - O(6')	2.68 ± 0.02 (4)	Al(2) - O(4')	1.966 ± 0.019 (2)	O(4) –O(5)	3·03 ± 0·03 (1)	TiO(3)	1.952 ± 0.018 (2)
O(1) - O(6'')	2.69 ± 0.02 (4)	O(5) - O(4')	2.55 ± 0.03 (2)	O(5) –O(6)	2·87 ± 0·03 (1)	O(2)-O(3)	2·57 ± 0·02 (2)
O(1) - O(1'')	2.91	O(3) - O(5)	2.72 ± 0.03 (2)	O(4) –O(6)	2·87 ±0·03 (1)	O(2)-O(4)	2·59 ± 0·03 (2)
		O(3) - O(4')	2.73 ± 0.03 (2)	O(6) –O(6')	2.91	O(1)-O(2)	2·92 ± 0·02 (2)
NaO(2)	2.57 ± 0.02 (4)	O(2') - O(5)	2.73 ± 0.03 (2)			O(1)-O(3)	2.82 ± 0.02 (2)
Na - O(5)	2.49 ± 0.02 (2)	O(2') - O(4')	2.59 ± 0.02 (2)			O(3)-O(4)	2.84 ± 0.03 (2)
O(2) - O(2')	$4 \cdot 24 \pm 0 \cdot 03$ (2)	O(4) - O(4)	2.91			O(3)-O(3)	2.91
O(5) - O(2)	2.73 ± 0.02 (4)	O(5) - O(5)	2.91			O(2)-O(2)	2.91
O(5) - O(2')	4.26 ± 0.03 (4)						
O(2) = O(2)	2.91 (2)						



Fig. 3. Structure of NaTi₂Al₅O₁₂. Al(1), Al(2), O(2), O(3) and O(6) and their symmetry related equivalents are at z=0, while Na, Al(3), Ti, O(1), O(4) and O(5) are all at $z=\frac{1}{2}$.

one string containing Ti, the other Al(2). They are represented by line shading in Fig.4. The double groups join by common corners to form stepped sheets normal to the b axis, and adjacent sheets are staggered relative to each other. Union between them is effected by the third octahedron centred about Al(1) (stippled in Fig. 4) sharing corners with those centred about Ti from two different sheets. In cross-section each octahedron containing either Ti or Al is joined to others centred about metal atoms of the other kind. Al(3) is tetrahedrally coordinated, and the bond distances to oxygen of 1.75, 1.79 and 1.83 Å are normal (International Tables for X-ray Crystallography, 1962, p. 262). The nearest neighbour metal atoms to it are all aluminum. This arrangement leaves a series of irregular holes, which as we have already discussed in some detail, accommodate Na in an octahedral environment. This is very similar to the one it adopts in rhombohedral α -NaFeO₂ (Goldsztaub, 1935).

Although this unusual structure has no close overall similarities to any known types, the double strings appear in a wide variety of oxides containing the transition metals. Particularly noteworthy are their presence in two aluminum compounds, AlOOH (diaspore; De-



Fig.4. NaTi₂Al₅O₁₂ showing the double octahedral strings in cross-section, the more heavily shaded ones being Ti, the lighter Al. These are bridged by the stippled octahedra enclosing Al, while the larger hatched circles are Na and the smaller are tetrahedral Al.

flandre, 1932) and θ -Al₂O₃ which is isomorphous with β -Ga₂O₃ (Geller, 1960). In the former the double strings form open tunnels which presumably enclose the protons, whereas in the latter they are joined through tetrahedrally coordinated ions.

The presence of these two coordination polyhedra in NaTi₂Al₅O₁₂, together with the presence of both triand quadri-valent elements, suggested to us that it might be the progenitor of a family of isomorphous phases formed by ionic substitution. The replacement of Al by Fe³⁺ could lead to magnetically interesting compounds; for example NaTi₂Fe₅O₁₂ might be expected to have Fe in two different coordination modes, while in NaGe₂Fe₅O₁₂ the Ge could be confined to the tetrahedra with all the Fe octahedral. Attempts to synthesize these compounds by a variety of techniques, however, have so far proved unsuccessful.

References

- ANDERSSON, S. & WADSLEY, A. D. (1962a). Acta Cryst. 15, 194.
- ANDERSSON, S. & WADSLEY, A. D. (1962b). Acta Cryst. 15, 201.
- BAYER, G. & HOFFMANN, W. (1965). Z. Kristallogr. 121, 9.
- BERTAUT, F. & BLUM, P. (1954). C.r. Acad. Sci. Paris, 239, 429.
- CRUICKSHANK, D. W. J., PILLING, D. E., BUJOSA, A., LOV-ELL, F. M. & TRUTER, M. R. (1961). In Computing Methods and the Phase Problem in X-ray Crystal Analysis, p. 32. Oxford: Pergamon Press.
- DALY, J. J., STEPHENS, F. S. & WHEATLEY, P. J. (1963). Monsanto Research S.A., Final Report no. 52.
- DEFLANDRE, M. (1932). Bull. Soc. franç. Minér. Crist. 55, 140.
- GELLER, S. (1960). J. Chem. Phys. 33, 676.
- GOLDSZTAUB, S. (1935). Bull. Soc. franç. Minér. Crist. 58, 6. International Tables for X-ray Crystallography (1962). Vol. III. Birmingham: Kynoch Press.
- MUMME, W. G. & REID, A. F. (1967). Acta Cryst. Submitted for publication.
- Théry, J., Lejus, A. M., BRIANÇON, D. & COLLONGUES, R. (1961). Bull. Soc. chim. Fr. p. 973.
- WADSLEY, A. D. (1964). In Non-Stoichiometric Compounds, edited by L. Mandelcorn, p. 111 et seq. New York: Academic Press.